

4-critical planar graphs with four triangles

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By the Grünbaum-Aksenov Theorem (extending Grötzsch's Theorem) every planar graph with at most three 3-cycles is 3-colorable. However, there are infinitely many planar 4-critical graphs with exactly four 3-cycles. We describe all such graphs. This answers a question of Erdős from 1990.